

# Multiple-Profile Prediction-of-Use Games

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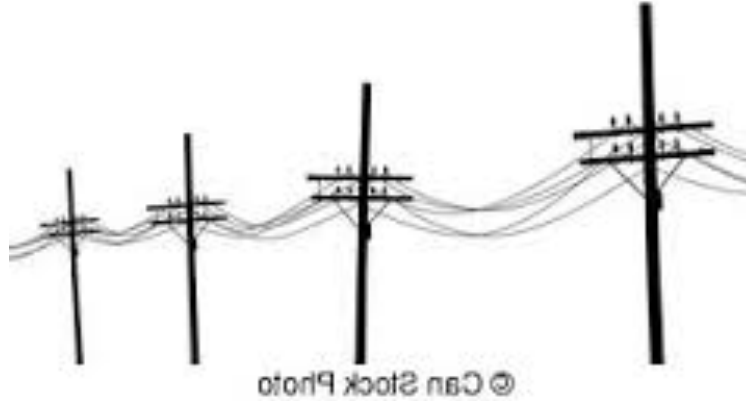


Computer Science  
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# Electricity Market



**Consumer** pays per kWh used, a *fixed-rate tariff*



**Supplier** buys electricity in advance, but can also buy at the last minute for a higher price



**Generator**

**Misalignment of incentives:** Consumer's cost does not depend on predictability, but supplier's cost does

# Prediction-of-Use (POU) Tariffs

- Each consumer makes a prediction ahead of time
  - They are charged based on:
    - How much they consume
    - How accurate their prediction was
- Consumers can form groups and be treated as one large consumer
  - But they can only do this if they can agree on how to split the costs

# Contributions

- Extend POU games to support multiple profiles
  - Extension remains convex
  - Creates new enforcement problems addressed by separating functions
- Experimentally validate our approach using learned utility models

# Intro to Cooperative Games

# Cooperative Games

- Set of agents  $N$
- Can form *coalitions*
  - Characteristic value function  $v: 2^N \rightarrow \mathbb{R}$  represents value each coalition can achieve
- Agents can defect to other coalitions, but are forced to cooperate within coalition
  - Coalition can enforce contracts
- Definition (*superadditivity*):  $v(S \cup T) \geq v(S) + v(T)$ 
  - *Grand coalition* of all agents maximizes utility

# Benefit Sharing

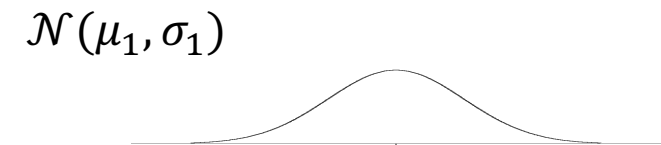
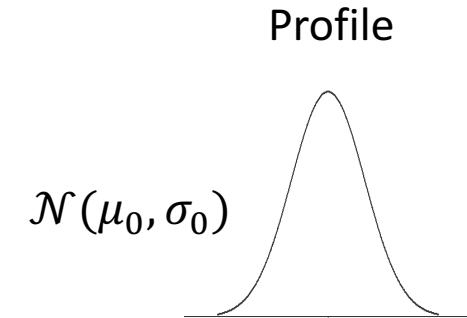
- Challenge: how to share benefits among its members?
- Def. (*stability*): no agent has incentive to defect to another coalition
- Two major approaches:
  - Core allocation: strong stability guarantees, but hard computation
  - Shapley value: fairness, “easy” to approximate, no stability guarantee
- If game is *convex* (has a supermodular characteristic function):
  - Shapley value (and some approximations) is a core allocation (Shapley, 1971)
  - Can cheaply get fairness of Shapley value and stability of core simultaneously

# Prediction-of-Use Games



# Robu et al. (2017) POU Model

- Each household has a distribution over consumption in *next time period*—a *profile*
- Households can form coalitions
  - Coalition's profile is sum of members' profiles
- Each coalition predicts a *baseline*  $b \in \mathbb{R}$



Valentin Robu, Meritxell Vinyals, Alex Rogers, and Nicholas Jennings. Efficient Buyer Groups with Prediction-of-Use Electricity Tariffs. *IEEE Transactions on Smart Grid* (2017).

# Robu et al. (2017) POU Model

- Three-parameter *POU tariff*:
  - Charge  $p$  for *realized consumption*
  - Charge  $\bar{p}$  for each unit over baseline  $b$
  - Charge  $\underline{p}$  for each unit under baseline  $b$
- Closed-form for optimal  $b$
- Characteristic function is total cost in expectation
- **Characteristic function is convex**

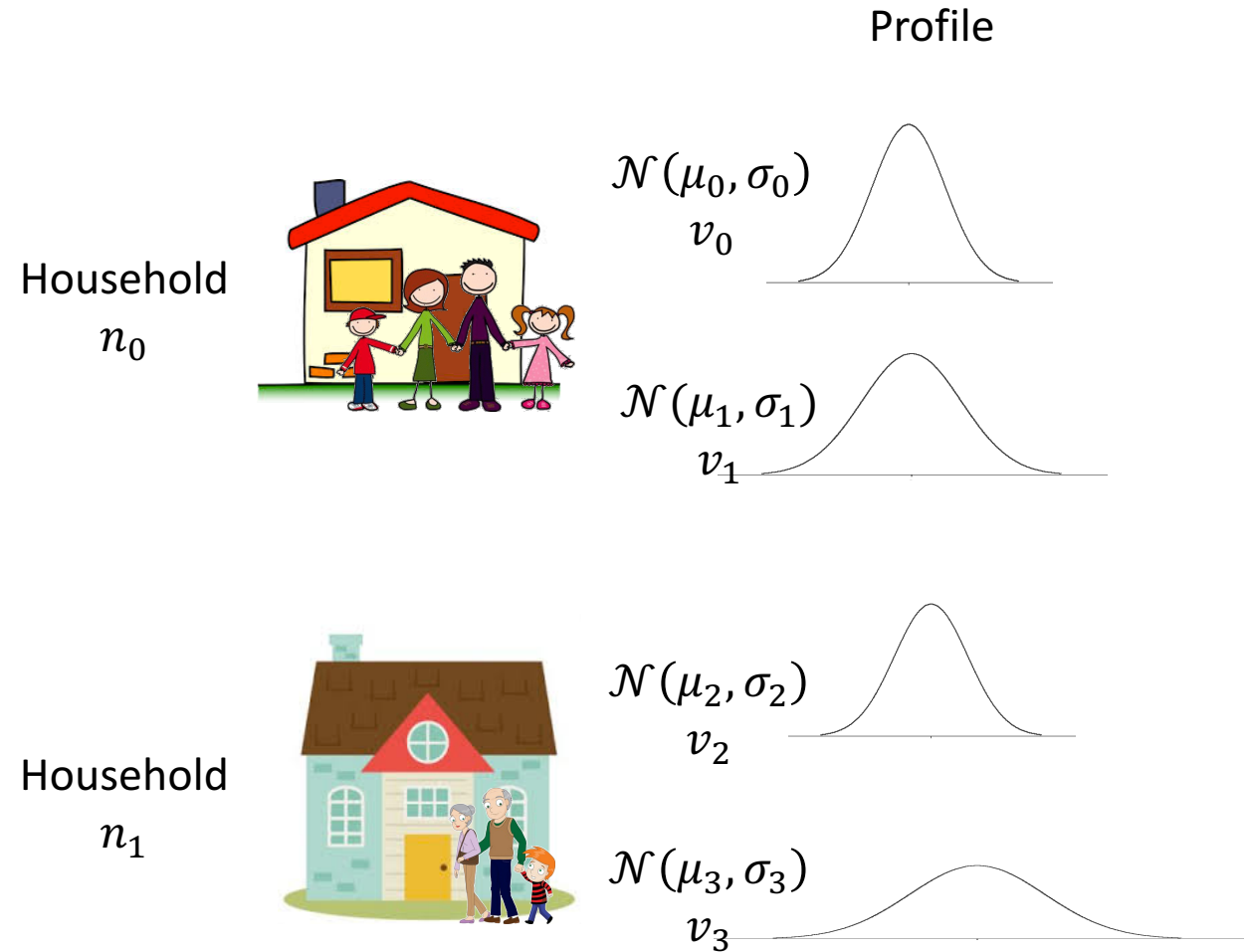
# Limitations of POU Games

- The only decision agents have in POU games is what profile to declare
- The choice of profile is made before the game starts
- Agents have utility functions—choosing the best profile is an optimization
- Optimal choice depends on what other agents choose

# Multiple-Profile Prediction-of-Use Games

# Multiple-Profile POU (MPOU) Games

- Each profile has a value
- Each household is assigned a profile by the coalition
- Characteristic function (value of a coalition):  
sum of assigned profile values  
minus expected costs, under  
best possible assignment



# Cost Sharing in MPOU Games

- Theorem: MPOU games are convex
- Additional complexity does not interfere with convexity 😊
- However, having multiple profiles creates a new issue

# Enforceability

- Coalition assigns a profile to each agent
- Actions are only partially observable in MPOU
  - Coalition knows each agent's profiles
  - *Selected* profile only known to agent
  - Coalition observes *realized* consumption

# Separating Functions (SFs)

- A *separating function* maps realized consumption to a payment
  - From coalition to agent
  - To incentivize use of the assigned profile
- Definition:  $D(x)$  is a separating function under assignment  $A$  of agents to profiles if:
  - $\mathbb{E}_{A(i)}(D(x)) + v(A(i)) > \mathbb{E}_{\bar{A}(i)}(D(x)) + v(\bar{A}(i))$  (incentive)
  - $\mathbb{E}_{A(i)}(D(x)) = 0$  (zero-expectation)



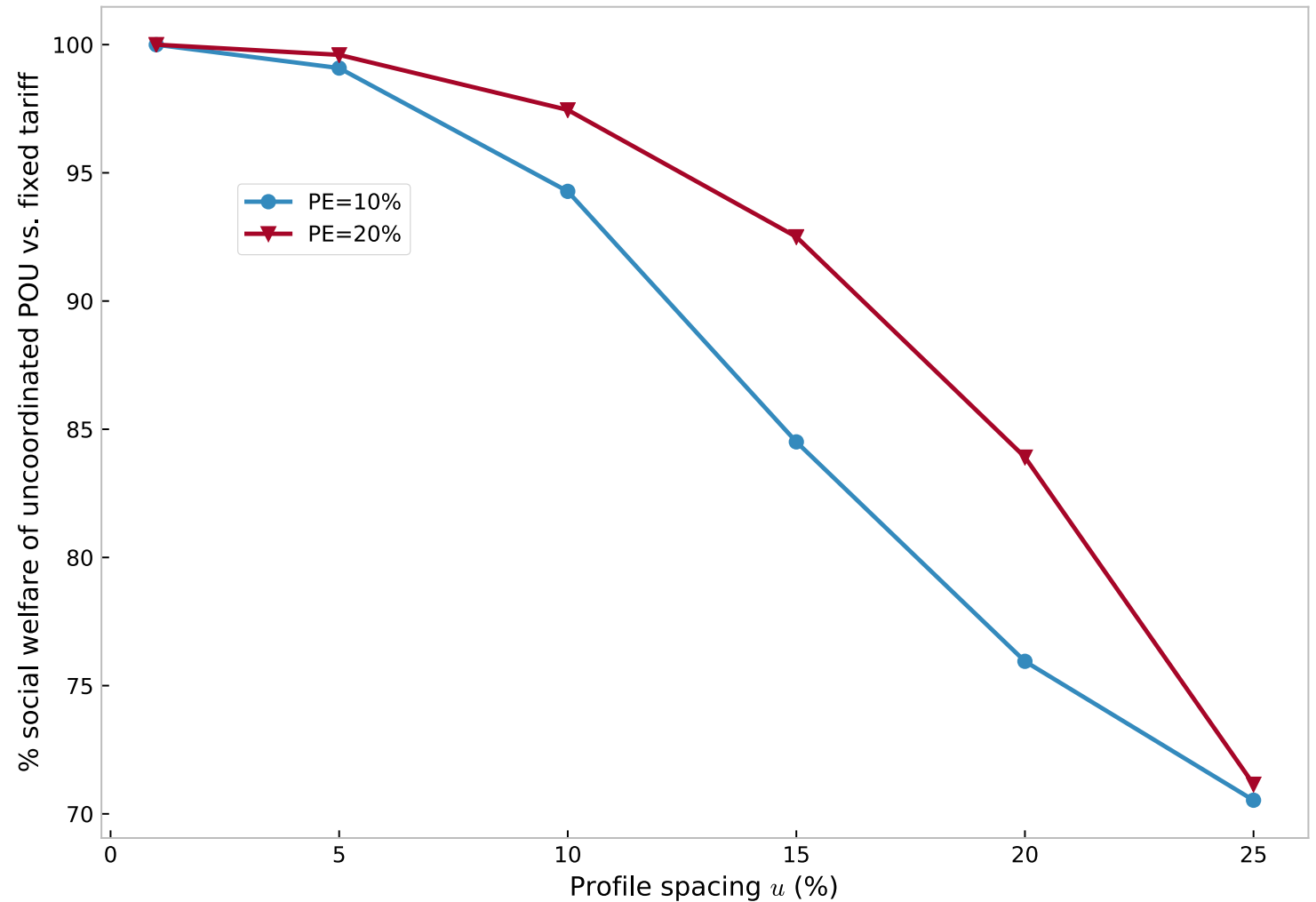
# Empirical Results

# Goal of Experiments

- Measure social welfare difference between POU, MPOU and fixed-rate tariff
  - Use agent utility functions learned from [pecanstreet.org](http://pecanstreet.org) data

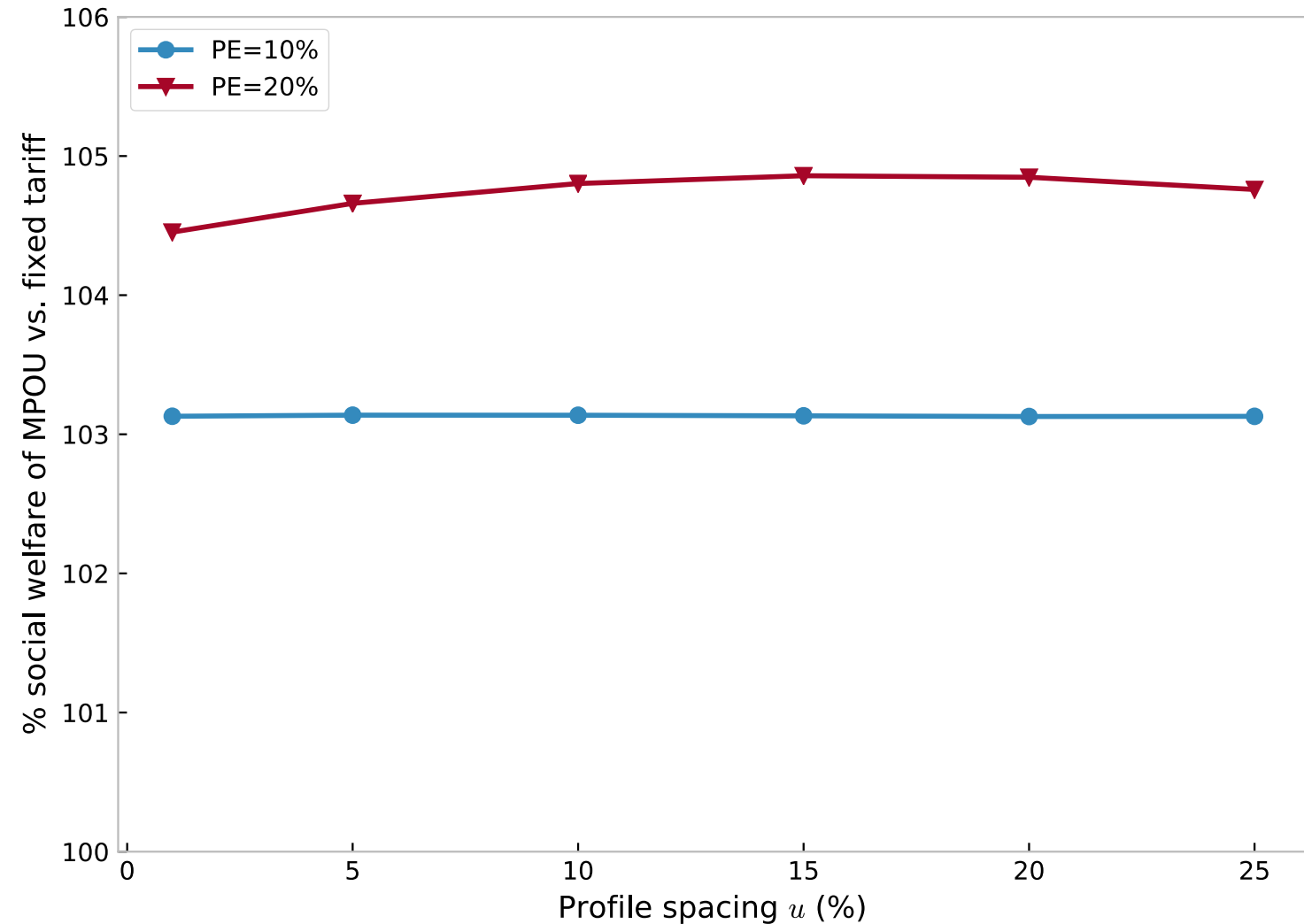
# Social Welfare: POU vs. Fixed-Rate

- POU suffers a large SW loss vs. fixed due to lack of coordination



# MPOU vs. Fixed-Rate

- MPOU shows a modest SW gain over fixed



# Contributions

- Extend POU games to support multiple profiles
  - Extension remains convex
  - Creates new enforcement problems addressed by separating functions
- Experimentally validate our approach using learned utility models
  - Social welfare:  $\text{POU} < \text{fixed-rate} < \text{MPOU}$

# Future Work

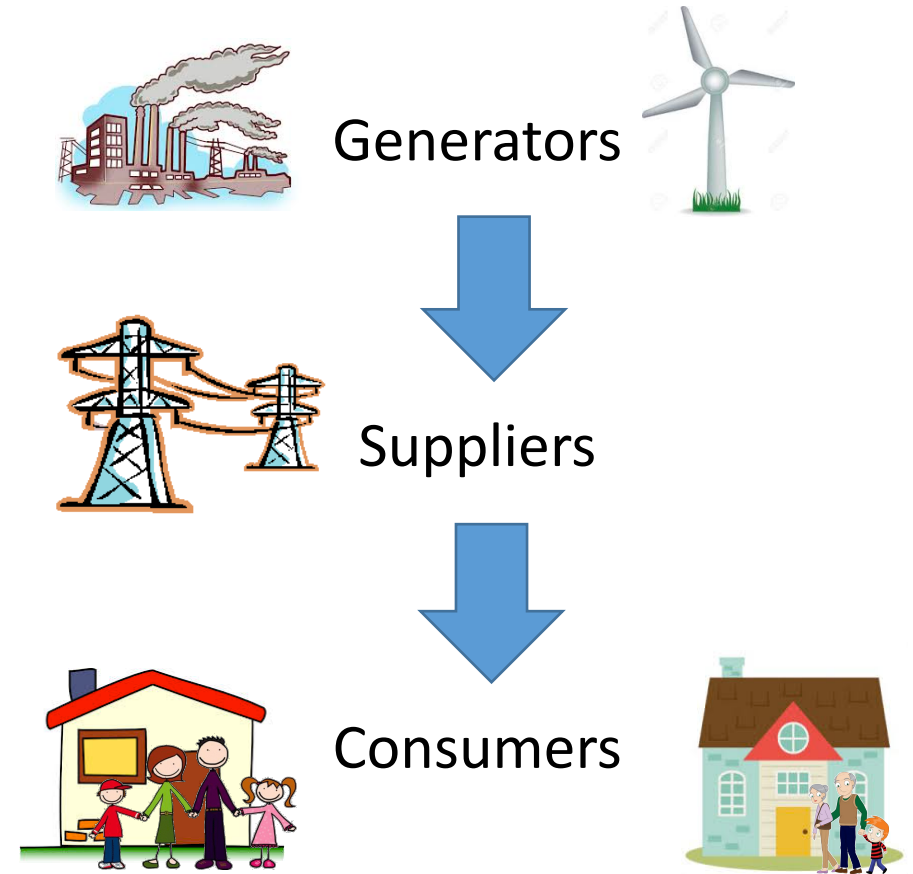
- POU games:
  - Manipulation
  - Correlated prediction errors
- Separating functions:
  - General applicability to principal-agent problems

# Thank You

- Poster #1938

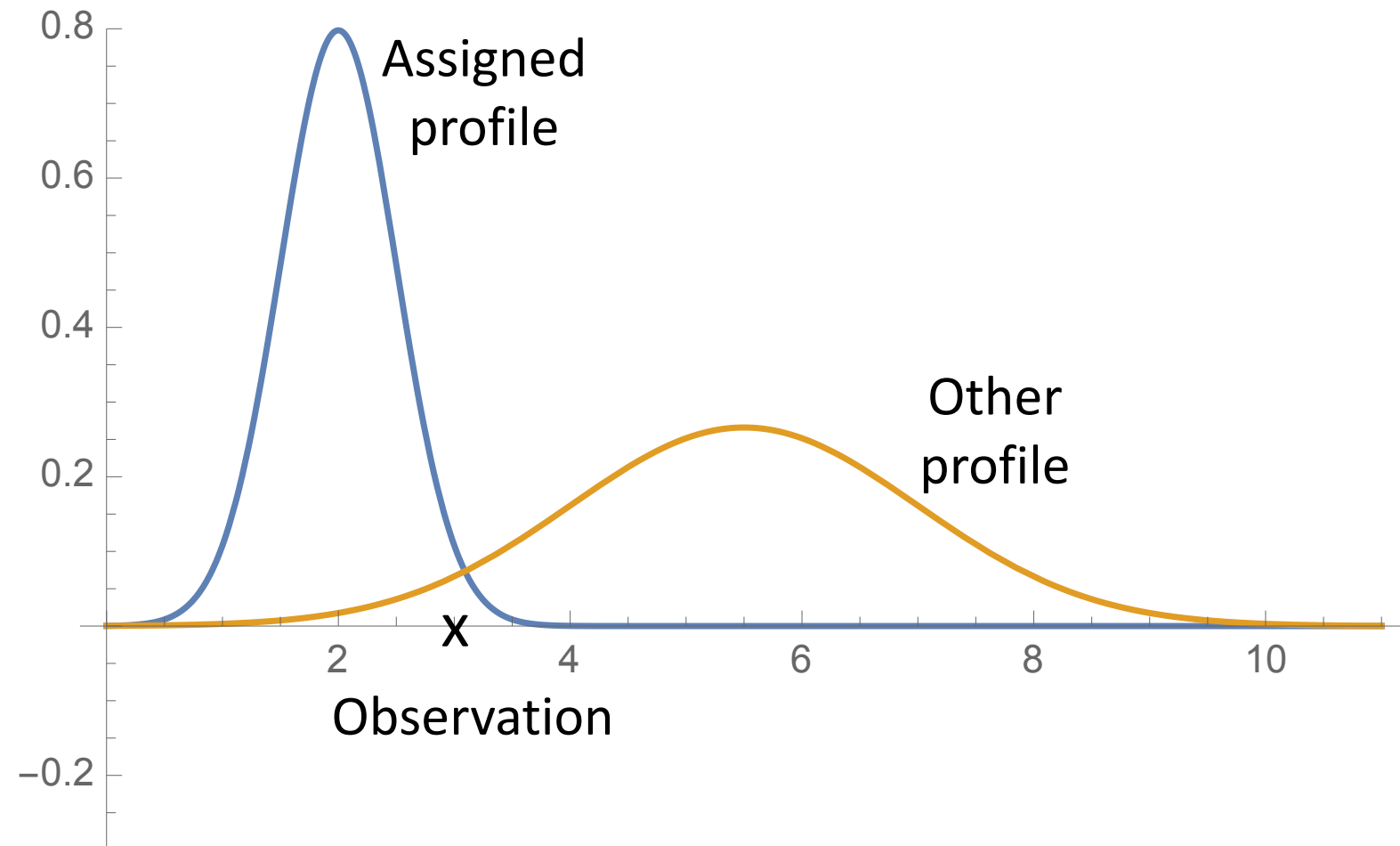
# Electricity Markets

- Electricity consumption is hard to predict for suppliers
- Predictable consumers are cheaper to serve
- Residential consumers face a fixed-rate tariff
  - They are not incentivized to be predictable





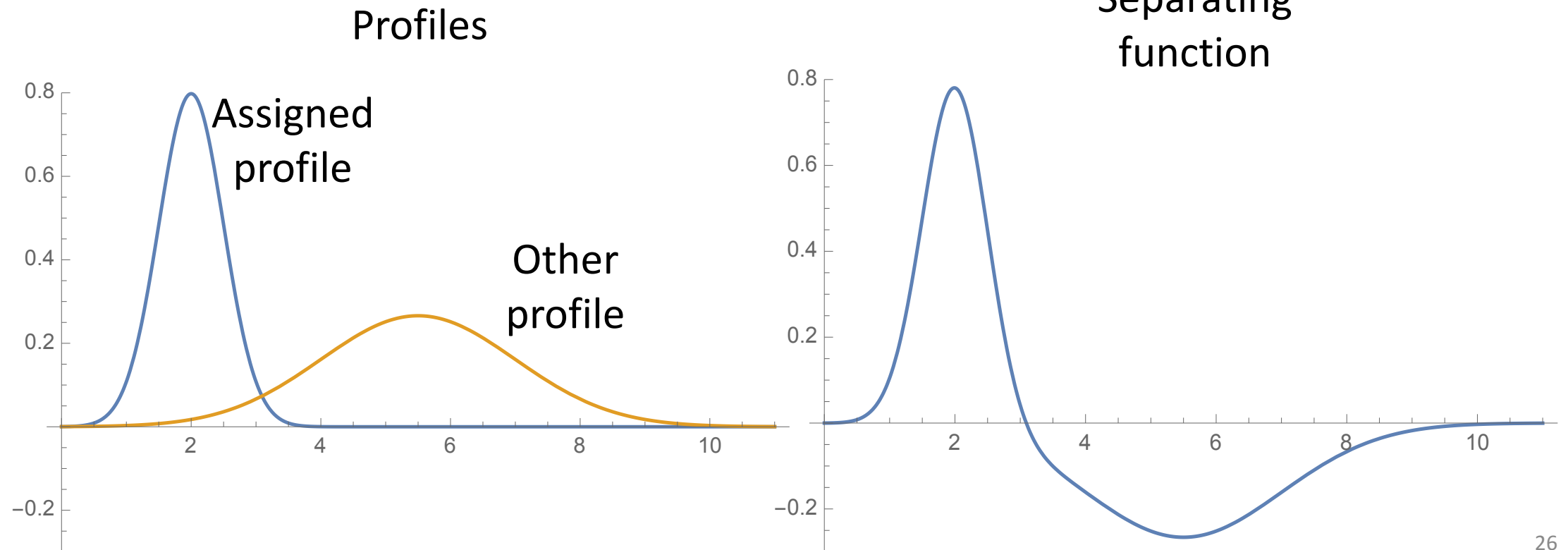
# SF Calculation, Two-Profile Example



# SF Calculation, Two-Profile Example

- Theorem: separating function for two-profiles:

$$\text{PDF}(\text{assigned profile}) - \text{PDF}(\text{other profile})$$



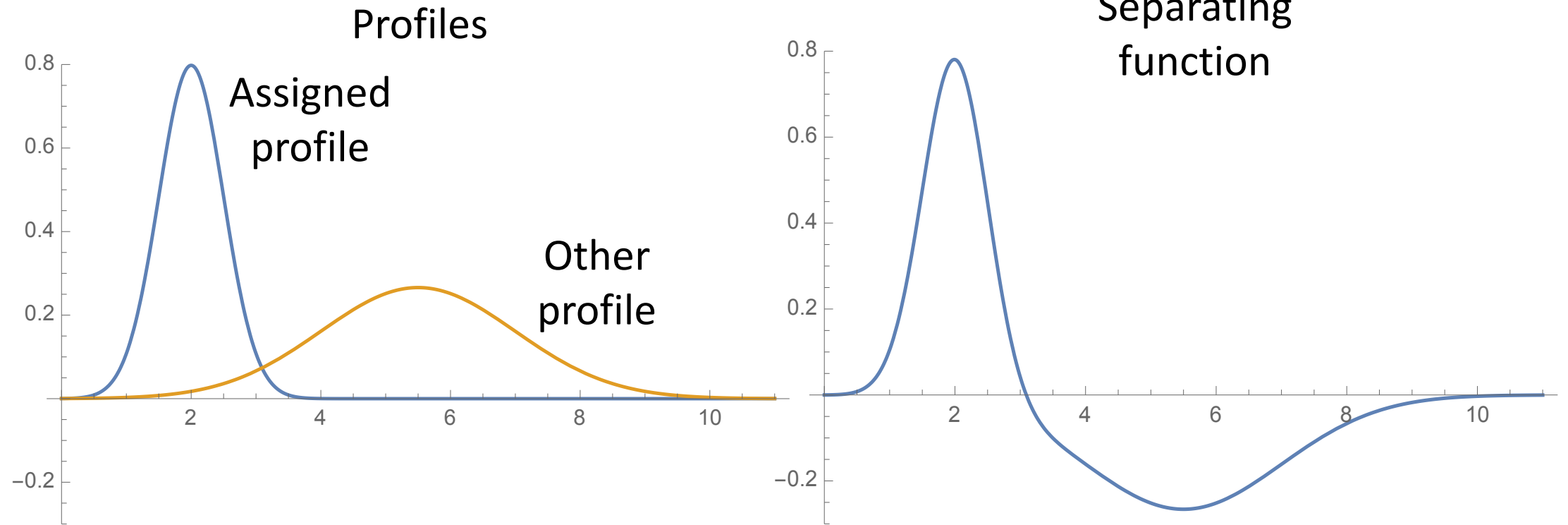
# SF Calculation, Arbitrary Number of Profiles

- No closed form that we know of
- Can compute using a linear program
- We suspect they always exist in practice

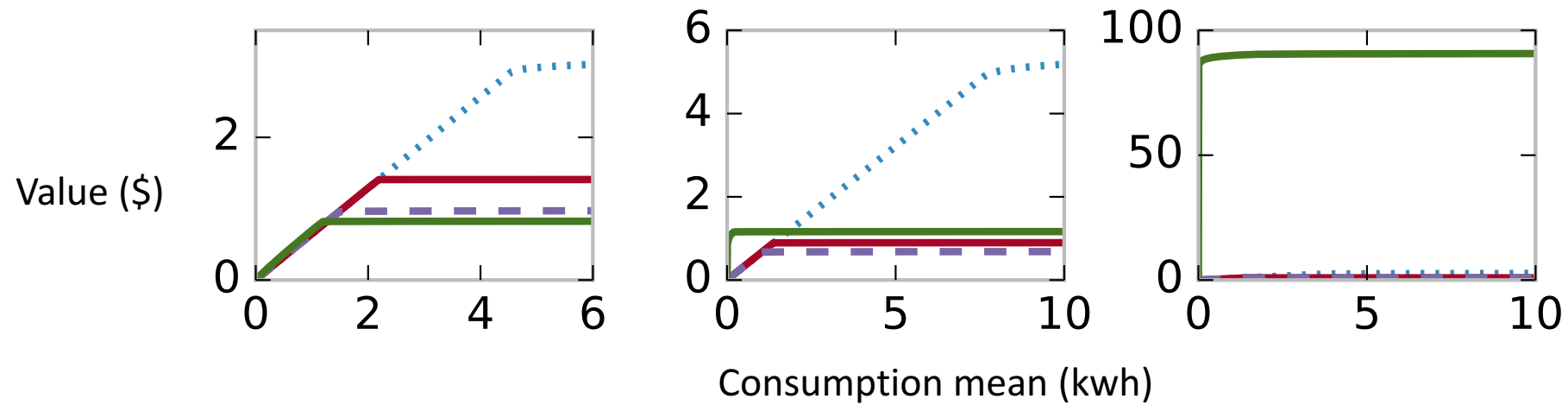
# Addressing the Problems of Weak SFs

- Key observation: weak separating condition maintained under affine transformations
  - A weak separating function can have arbitrary power through scaling
  - Can make  $\mathbb{E}_{A(i)}(D(x)) = 0$  through translation. Thus, payments not affected

# SFs Introduce Variance



# Utility Models



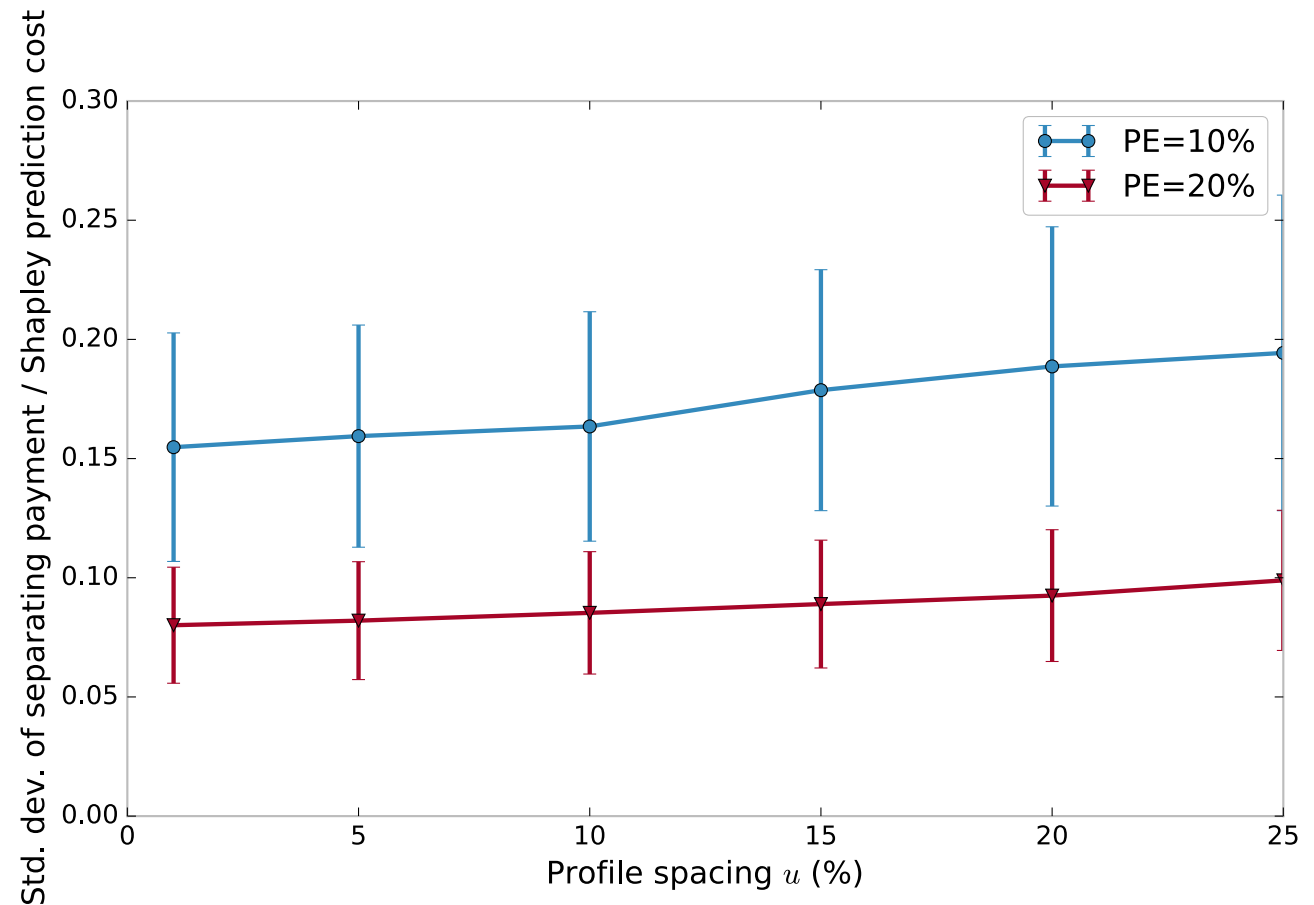
Free for academic use at [pecanstreet.org](http://pecanstreet.org)

# Instance Generation

- Generate agents by sampling utility functions
- Create revenue-equivalent fixed-rate and POU tariffs
  - *Predictivity emphasis (PE)*: parameter for how much agents are penalized for prediction errors relative to fixed-cost
- Generate profiles for each agent
  - *Profile spacing*: measure of how dissimilar generated profiles are

# Variance Introduced by SFs

- Record average variance of SF as a fraction of Shapley payment
  - Only for agents that require SFs (1-10%) of total
- Substantial variance introduced
- If time periods are independent, variance decreases in aggregate





# Core Allocations

- Let  $t(i)$  be the payment to agent  $i$
- *Budget balance*: distributes all benefits:  $\sum_{i \in N} t(i) = v(N)$
- *Stability*: no defections possible:  $\forall S \subset N, \sum_{i \in S} t(i) \geq v(S)$
- Very satisfying, but, in general:
  - May not exist
  - May be hard to compute

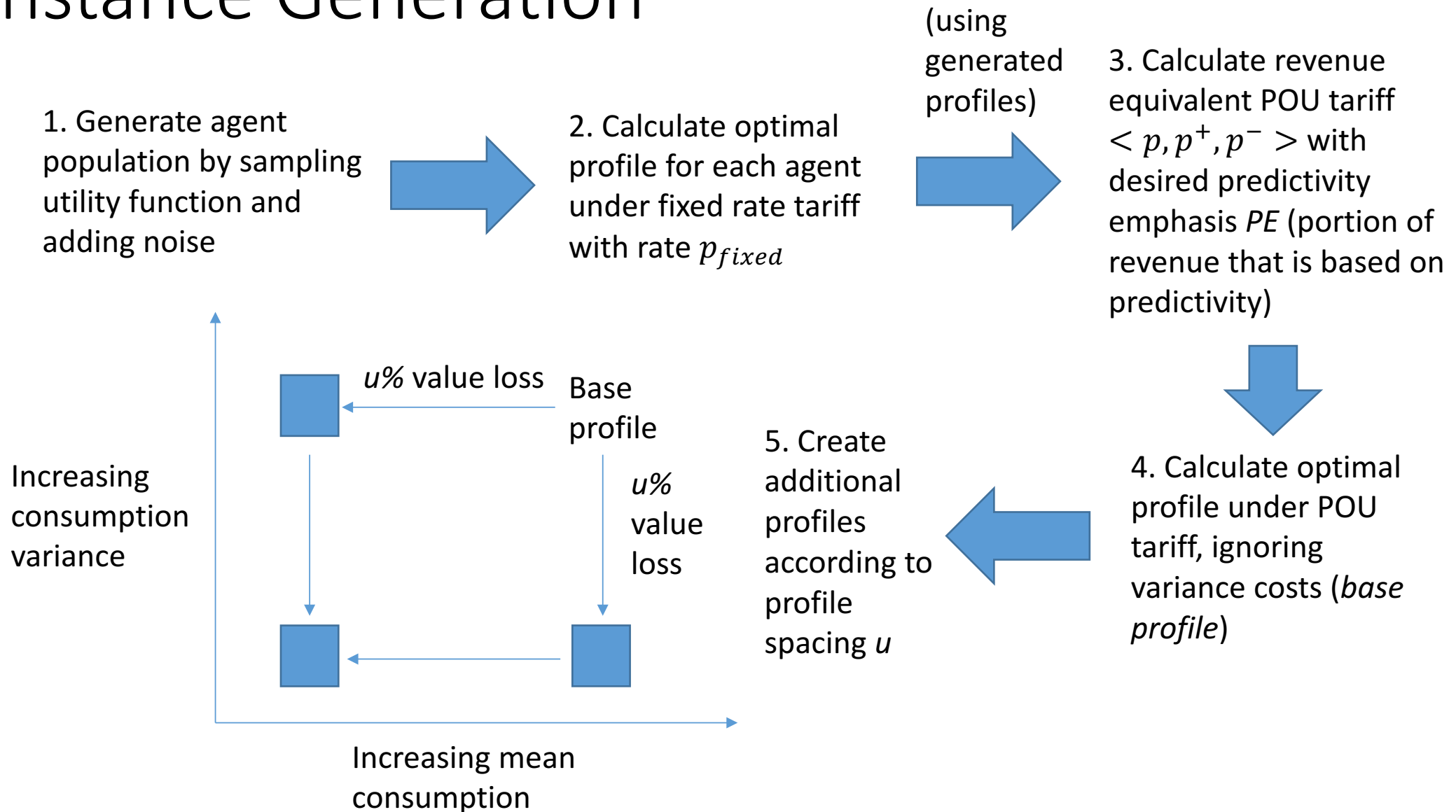
# Shapley Value

- Intuition: agent's average contribution to coalition value
- Guarantees “fairness”
- Budget-balanced, but not guaranteed to be stable
- Easy to approximate
- If a

# Scalability

- 100k agents with 4 profiles each takes 90 minutes
- Largest bottleneck is Shapley value computation:  $n \log n$  linear programs (LPs) where  $n$  is number of agents
  - Each LP has  $nk$  variables where  $k$  is number of profiles
  - Need to calculate coalition values  $n$  times for each sample
  - Need  $\log n$  samples
- Separating function LPs have  $k^2$  variables each

# Instance Generation



# Profile Spacing

- Base profile maximizes utility ignore variance → only need to consider profiles that reduce variance
- But we don't know what spacing will maximize social welfare (SW)

